

## NUT RIGIDITY

The calculations necessary to determine the rigidity of the ball zone are very involved. However the following approximation will give a value that is sufficiently accurate for most purposes.

For double ball nut assemblies, preloaded to one tenth of the Dynamic Capacity, the rigidity can be approximated by using the equation:

$$R_z \approx 10 \cdot d_o \cdot i$$

where

$R_z$  = rigidity of ballzone (N/μm)

$d_o$  = nominal diameter of ballscrew (mm)

$i$  = number of rows of balls in one nut

For single ball nuts the rigidity may be approximated by:

$$R_z \approx 5 \cdot d_o \cdot i$$

## OVERALL SYSTEM RIGIDITY

The overall rigidity is calculated by the following formula:

$$\frac{1}{R} = \frac{1}{R_s} + \frac{1}{R_n} + \frac{1}{R_b} + \frac{1}{R_h}$$

where

$R$  = overall rigidity (N/μm)

$R_s$  = rigidity of screw shaft (N/μm)

$R_n$  = rigidity of nut (N/μm) which normally  $\approx 0.8 \cdot R_z$

$R_b$  = rigidity of bearings (N/μm)

$R_h$  = rigidity of nut mounting and bearing housings (N/μm)

Exact calculation to DIN 69051 (Part 6)

## MATERIALS

JENA-TEC use high quality steels, specially processed to ensure high performance product.

Ballshafts: Inductively hardened tempered steel Cf 53 balltrack hardened to  $60 \pm 2$  HRC. Core and spindle ends non-hardened.

Ballnuts: Case hardened steel 16MnCr5 or roller-bearing steel 100Cr6.

Note: Special materials and stainless steels can be supplied as required. Please discuss your requirements with JENA-TEC Engineers.

## STATIC LOAD RATING

Static load rating  $C_o$ : is the centred axial load under which the permanent combined deformation of balls and tracks at the most heavily loaded point on the ballscrew drive is 1/10000 of the ball diameter.

Note: The figure for maximum static load, beyond which brinelling of the balltrack will occur, is given in the ballscrew data sheets.

## DRIVING TORQUE REQUIREMENTS

The torque which must be applied to a ballscrew in order to produce an axial thrust is given by:

$$T = \frac{F \cdot Ph_o}{2 \cdot 10^3 \cdot \pi \cdot \eta}$$

$$\text{which} = \frac{F \cdot Ph_o}{5655} \text{ when } \eta = 0.9$$

where

$T$  = torque (Nm)

$F$  = axial thrust load (N)

$Ph_o$  = lead (mm)

$\eta$  = efficiency of the ballscrew

To this the torque due to drag from preloading, wiper seals, and inertia of the ballscrew shaft should be added.

The preload drag torque may be calculated from the following:

$$\max T_p = \frac{0.004 \cdot d_o \cdot F_p}{1000}$$

where

$T_p$  = dynamic preload drag torque (Nm)

$F_p$  = preload (N)

$d_o$  = nominal diameter of ballscrew (mm)

The preload drag torque will decrease as the external load is applied and can be ignored if the applied load is three times that of the preload.

The torque required to overcome the inertia of the ballscrew shaft, assuming constant acceleration, is given by the following formula:

$$T_1 = \frac{0.08 \cdot 10^{-12} \cdot d^4 \cdot L \cdot n}{t}$$

where

$T_1$  = torque to overcome inertia (Nm)

$d$  = average dia. of ballscrew shaft (mm)  
(shaft outside dia + root dia)  $\cdot 0.5$

$L$  = length of ballscrew (mm)

$n$  = maximum rotational speed (min<sup>-1</sup>)

$t$  = time taken to start or stop (sec)

**Note:** When a mass is being moved, it is important that acceleration and deceleration forces are taken into account in calculating the axial load on the ballscrew.

**SERVICE LIFE / LIFE EXPECTANCY**

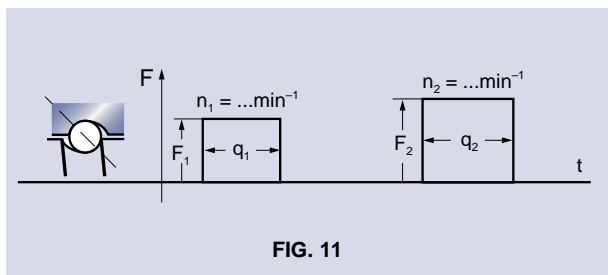
The use of correctly treated high grade steels and attention to detail mean that long life and trouble free operation can be expected from JENA-TEC ballscrews. It is important that the design, application, installation and maintenance procedures are correctly followed to achieve maximum service life. Assuming the above criteria are met the calculations are as follows:

The estimated service life of a ballscrew can be calculated as follows:

$$L = \left( \frac{Ca}{Fm} \right)^3 \cdot 10^6$$

where

- L = the estimated life in revolutions achieved or exceeded by 90% of an appropriately large number of identical ballscrew drives before the first signs of material fatigue.
- Ca = the dynamic load rating (N)
- Fm = the equivalent applied load (N). Loads can act on a ballscrew drive in two directions. Fm should be determined for each of the load directions; the larger value should then be used in the calculation of L. It is useful to draw a schematic diagram as (Fig 11), it should be noted that any preloading represents a continuous load.



**FIG. 11**

From Fig 11

$n_m$  = Mean speed

$$n_m = \frac{n_1 \cdot q_1 + n_2 \cdot q_2 + \dots + n_n \cdot q_n}{100}$$

$$F_m = \left( \frac{F_1^3 \cdot n_1 \cdot q_1}{n_m \cdot 100} + \frac{F_2^3 \cdot n_2 \cdot q_2}{n_m \cdot 100} + \dots \right)^{1/3} \cdot f_a$$

where

- $q_1, q_2$  = the components of the duration of a load in one direction in %.  
( $q_1 + q_2 + \dots + q_n = 100\%$ )
- $n_1, n_2$  = the speeds during  $q_1, q_2$  (rpm)
- $F_1, F_2$  = the axial load in N in one load direction during  $q_1, q_2$
- $f_a$  = the machine specific allowance.
- $f_a = 1$  for low acceleration values and no vibration
- $f_a = 1.5$  for higher acceleration and with vibration and medium impact loads

Please consult JENA-TEC in the case of impact loads exceeding  $0.5 \cdot Ca$ .

Ballscrew drive with preloaded nut system:

In cases where preloaded nut systems are used, the above calculations are used to determine the service life of each individual nut in both load directions. The overall service life is then calculated as follows:

$$L = (Fm1^{10/3} + Fm2^{10/3})^{-0.9} \cdot Ca^3 \cdot 10^6$$

where

- L = the overall service life (as above)
- Fm1 or Fm2 = the load of the nut 1 or 2 in the relevant load direction
- Ca = the dynamic load rating (N)

**Important Note:** The calculations above are valid only with correct lubrication. The presence of dirt, or lubrication starvation may reduce service life to a fraction of the calculated value. Reduced service life must also be expected with very short strokes.

Ballscrew nuts cannot absorb radial forces or tilting moments.

**LEAD ACCURACY**

JENA-TEC precision ballscrews are manufactured to an international grading system as shown below or to customers' own specific requirements.

Permissible deviation Grade (IT)						
	1	3	4	5	7	10
Lead Accuracy						
per 300 mm	0.006	0.012	0.016	0.023	0.052	0.210
per foot	0.0002	0.0005	0.0006	0.0009	0.002	0.008
Total travel deviation						
length ≤ 1000	0.011	0.021	0.029	0.040	0.090	-
>1000 ≤ 2000	0.018	0.035	0.048	0.065	0.150	-
>2000 ≤ 3000	0.026	0.050	0.069	0.093	0.210	-

**Note:** Grade 1 is offered only by special arrangement. Grade 3-5 are normally acceptable for machine tool applications. Transport screws are generally not preloaded.

Specified Lead: Nominal leads may be modified to accommodate specific requirements. A minus compensation will, for example, accommodate for temperature or pre-tensioning in the shaft.

- Ground screws: are available in Grade 1 to Grade 7
- Rolled screws: are available in Grade 5 to Grade 10
- Cut screws: are available in Grade 7 to Grade 10